

Implementing the APA model for the symmetric Needham-Schroeder protocol in state transition pattern notation in the SH Verification Tool

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The protocol

1. $A \longrightarrow S : A, B, R_A$
2. $S \longrightarrow A : \{R_A, B, K_{AB}, \{K_{AB}, A\}_{K_{BS}}\}_{K_{AS}}$
3. $A \longrightarrow B : \{K_{AB}, A\}_{K_{BS}}$
4. $B \longrightarrow A : \{R_B\}_{K_{AB}}$
5. $A \longrightarrow B : \{R_B - 1\}_{K_{AB}}$

An APA model for the symmetric Needham-Schroeder protocol and a detailed explanation of that model is given in [SOR02]. Here a translation of a slightly modified version of that model into the syntax of the SH verification tool is shown.

The reachability graph for a simple protocol run computed by the tool is appended.

As a basis for the implementation the APA model as specified in the appendix of [SOR02] is used.

Corresponding syntax of the APA model and SH verification tool [Fra02b, Fra02a, ORR00] are shown side by side.

The complete specification in SH verification tool syntax is included in the appendix.

A short tour of SH Verification Tool syntax for APA state transition pattern notation:

Some examples used in the Needham-Schroeder model and their SH verification tool counterpart:

$$\begin{array}{ll} (start, B) \in State_A & ['start', B] ? A_State \\ (start, B) \leftrightarrow State_A & \text{tool syntax: } ['start', B] \ll A_State \\ (B, R_A, S) \leftrightarrow State_A & [B, R_A, S] \gg A_State \end{array}$$

Example 1: A simple preamble for the SH verification tool and the computed reachability graph:

A global state `multiset` is defined and initialised:

```
defset nat0_seq = seq(nat_0);
def_state multiset: nat0_seq := 2.3.3;
```

A role `role` is defined and bound to 'instance':

```
def_role role;
def_pattern_bind role := 'instance' ;
```

A transition pattern for that role just takes out one element from the global state `multiset`:

```
def_trans_pattern role pattern
(x)
x \ll multiset;
```

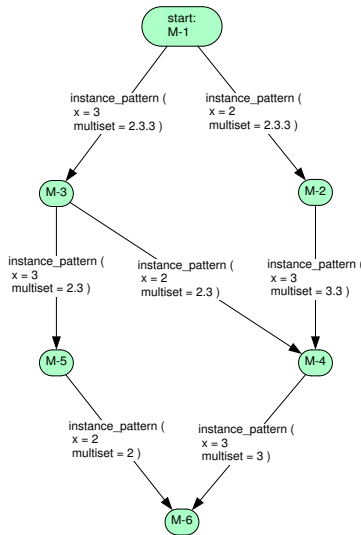


Figure 1: Reachability graph of example 1

Example 2: An example using a global state `network` and two instances of different roles one putting some information from local state `role1_my_set` into global state `network` and the other taking the data out of `network` into the local state `role2_my_set`.

```
defset nat0_seq = seq(nat_0);
def_state network: nat0_seq := ::;

def_role role1;
def_role role2;
def_pattern_bind role1 := 'instance1' ;
def_pattern_bind role2 := 'instance2' ;

def_state role1 my_set: nat0_seq := 2.3.3;
def_state role2 my_set: nat0_seq := ::;

def_trans_pattern role1 pattern1
(x)
x << role1_my_set,
network = ::, /* check whether network is empty */
x >> network;

def_trans_pattern role2 pattern1
(y)
y << network,
y >> role2_my_set;
```

Figure 2 shows the reachability graph computed by the SH Verification Tool for this example.

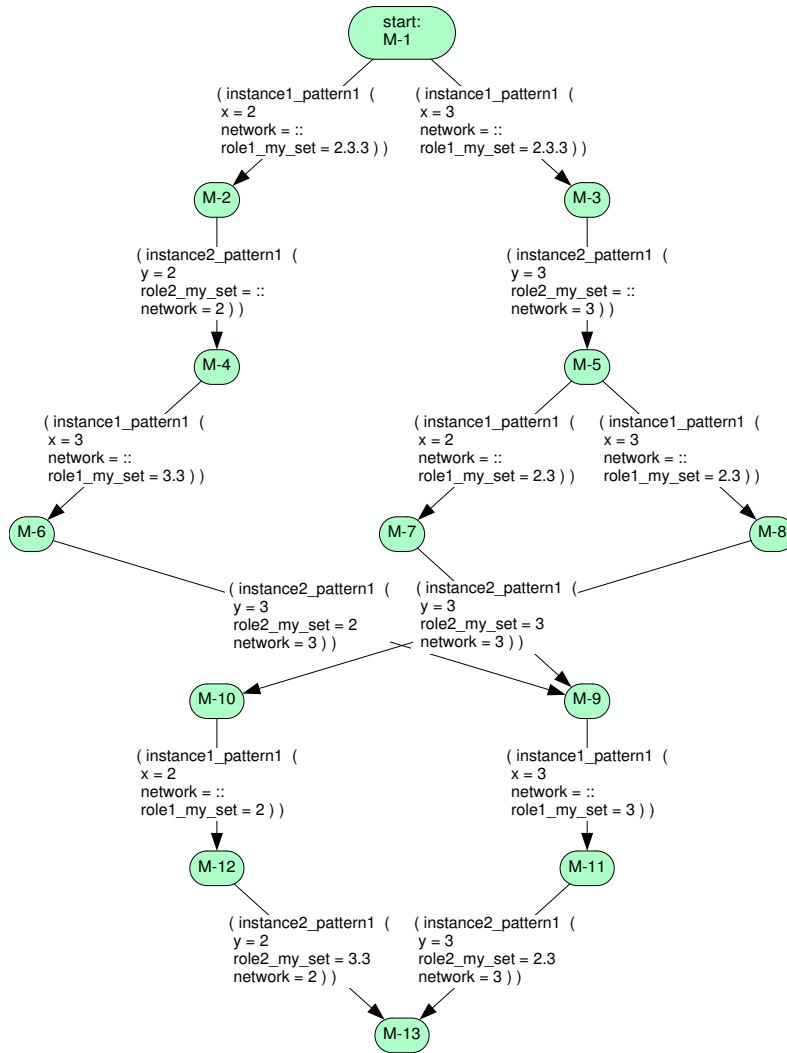


Figure 2: Reachability graph of example 2

Now the corresponding syntax of the APA model in [SOR02] and SH Verification Tool [Fra02b, Fra02a, ORR00] are shown side by side.

APA model (initial state):

$$\begin{aligned}
 \text{State}_A &:= \{(\mathbf{B}, \textit{agent}), (\mathbf{S}, \textit{server}), (\textit{start}, \mathbf{B})\} \\
 \text{Symkeys}_A &:= \{(\mathbf{S}, \textit{sym}, (\mathbf{A}, \mathbf{S}, \textit{sym}))\} \\
 \text{Asymkeys}_A &:= \emptyset \\
 \\
 \text{State}_B &:= \{(\mathbf{A}, \textit{agent}), (\mathbf{S}, \textit{server}), (\textit{respond}, \mathbf{A})\} \\
 \text{Symkeys}_B &:= \{(\mathbf{S}, \textit{sym}, (\mathbf{B}, \mathbf{S}, \textit{sym}))\} \\
 \text{Asymkeys}_B &:= \emptyset \\
 \\
 \text{State}_S &:= \{(\mathbf{A}, \textit{agent}), (\mathbf{B}, \textit{agent})\} \\
 \text{Symkeys}_S &:= \{(\mathbf{A}, \textit{sym}, (\mathbf{A}, \mathbf{S}, \textit{sym})), (\mathbf{B}, \textit{sym}, (\mathbf{B}, \mathbf{S}, \textit{sym}))\} \\
 \text{Asymkeys}_S &:= \emptyset \\
 \\
 \text{Network} &:= \emptyset
 \end{aligned}$$

SH Verification Tool:

```

def_role A;
def_role B;
def_role S;

def_state A State: Messages_seq := [B, 'agent'].[S, 'server'].['start', B];
def_state A Symkeys: Symkeys_seq := (S, 'sym', (A, S, 'sym'));
def_state A Asymkeys: Asymkeys_seq := :::

def_state B State: Messages_seq := [A, 'agent'].[S, 'server'].['respond', A];
def_state B Symkeys: Symkeys_seq := (S, 'sym', (B, S, 'sym'));
def_state B Asymkeys: Asymkeys_seq := :::

def_state S State: Messages_seq := [A, 'agent'].[B, 'agent'];
def_state S Symkeys: Symkeys_seq := (A, 'sym', (A, S, 'sym')).
                                   (B, 'sym', (B, S, 'sym'));
def_state S Asymkeys: Asymkeys_seq := :::

def_state Network: net_elem_seq := :::

def_pattern_bind A := 'Alice';
def_pattern_bind B := 'Bob';
def_pattern_bind S := 'Server';

```

APA model (step 1):Variables: R_A, B, S $(start, B) \in \text{State}_A$ $(B, agent) \in \text{State}_A$ $(S, server) \in \text{State}_A$ \xrightarrow{A} $R_A \in \text{new_nonce}$ $(start, B) \quad \leftrightarrow \quad \text{State}_A$ $(B, R_A, S) \quad \hookrightarrow \quad \text{State}_A$ $(A, S, (A, B, R_A)) \quad \hookrightarrow \quad \text{Network}$ **SH Verification Tool:**

```
def_trans_pattern A step_1
(RA,B,S)
['start',B] ? A_State,
[B,'agent'] ? A_State,
[S,'server'] ? A_State,
RA << new_nonce,
tail(RA) >> new_nonce,
['start',B] << A_State,
[B,head(RA),S] >> A_State,
(A,S,[A,B,head(RA)]) >> Network;
```

For the example `Nonces` are modeled in the tool by a list of `Nonce`. The state `new_nonce` initially contains a multiset (sequence) of one list of `Nonces`. Here we use only two nonces 13 and 17 needed for one run of the protocol in step 1 above and step 4.

```
defset Nonce = 13, 17, 19, 23;
defset Nonces = [Nonce];
defset Nonce_seq = seq(Nonces);
def_state new_nonce: Nonce_seq := [13,17];
```

In the pattern above `RA` is bound to the list `[13,17]`, the single element of the multiset `new_nonce`, then the tail of `RA` (in this case `[17]`) is put back into the multiset and the head of `RA` (in this case `13`) is used in the further lines of the above pattern.

In a concrete implementation a pseudo-random number generator should be used to generate nonces.

APA model (step 2):

Variables: $X, A, B, M, K_{AS}, K_{BS}, K_{AB}, R_A$

$(X, S, M) \in \text{Network}$
 $(A, \text{agent}) \in \text{State}_S \wedge \text{elem}(1, M) = A$
 $(B, \text{agent}) \in \text{State}_S \wedge \text{elem}(2, M) = B$
 $(A, \text{sym}, K_{AS}) \in \text{Symkeys}_S$
 $(B, \text{sym}, K_{BS}) \in \text{Symkeys}_S$
 \xrightarrow{S}
 $R_A := \text{elem}(3, M)$
 $(A, B, \text{sym}) \in \text{new_key}$
 $K_{AB} := (A, B, \text{sym})$
 $(X, S, M) \quad \leftrightarrow \quad \text{Network}$
 $(S, A, (\text{encrypt}(K_{AS}, (R_A, B, K_{AB},$
 $\text{encrypt}(K_{BS}, (K_{AB}, A)))))) \quad \leftrightarrow \quad \text{Network}$

SH Verification Tool:

```

def_trans_pattern S step_2
  (X,A,B,M,KAS,KBS)
  (X,S,M) ? Network,
  [A,'agent'] ? S_State,
  A = head(M),
  [B,'agent'] ? S_State,
  B = head(tail(M)),
  (A,'sym',KAS) ? S_Symkeys,
  (B,'sym',KBS) ? S_Symkeys,
  /* RA = head(tail(tail(M))), */
  (X,S,M) << Network,
  (S,A,encrypt(KAS,[head(tail(tail(M))),B,(A,B,'sym')],
  encrypt(KBS,[A,B,'sym'],A)))) >> Network;

```

In the tool the abbreviation RA used in the pattern above is currently not used. Instead $\text{elem}(3,M)$ is inserted directly notated here by $\text{head}(\text{tail}(\text{tail}(M)))$.

APA model (step 3):

Variables: $X, B, S, M, Chiffretext, K_{AS}, K_{AB}, R_A$

$(X, A, M) \in \text{Network}$
 $(B, R_A, S) \in \text{State}_A$
 $(S, sym, K_{AS}) \in \text{Symkeys}_A$
 $elem(1, decrypt(K_{AS}, M)) = R_A$
 $elem(2, decrypt(K_{AS}, M)) = B$
 \underline{A}
 $K_{AB} := elem(3, decrypt(K_{AS}, M))$
 $Chiffretext := elem(4, decrypt(K_{AS}, M))$
 $(X, A, M) \leftrightarrow \text{Network}$
 $(B, R_A, S) \leftrightarrow \text{State}_A$
 $(new\ session\ key, B, K_{AB}) \hookrightarrow \text{State}_A$
 $(A, B, Chiffretext) \hookrightarrow \text{Network}$

SH Verification Tool:

```
def_trans_pattern A step_3
  (X,B,S,M,KAS,RA)
  (X,A,M) ? Network,
/* [B,RA,S] ? A_State,*/
  (S,'sym',KAS) ? A_Symkeys,
  head(decrypt(KAS,M)) = RA,
  head(tail(decrypt(KAS,M))) = B,
  [B,RA,S] ? A_State,
/* KAB = head(tail(tail(decrypt(KAS,M)))) ,*/
/* Chiffretext = head(tail(tail(tail(decrypt(KAS,M))))),*/
  (X,A,M) << Network,
  [B,RA,S] << A_State,
  [new_session_key,B,head(tail(tail(decrypt(KAS,M))))] >> A_State,
  (A,B,head(tail(tail(tail(decrypt(KAS,M)))))) >> Network;
```

In the tool the abbreviations `KAB` and `Chiffretext` used in the pattern above are currently not used and the corresponding expression shown in the commented lines is inserted directly.

APA model (step 4):

Variables: $X, A, S, M, K_{BS}, K_{AB}, R_B$

$(X, B, M) \in \text{Network}$
 $(\text{respond}, A) \in \text{State}_B$
 $(A, \text{agent}) \in \text{State}_B$
 $(S, \text{server}) \in \text{State}_B$
 $(S, \text{sym}, K_{BS}) \in \text{Symkeys}_B$
 $\text{elem}(2, \text{decrypt}(K_{BS}, M)) = A$
 \xrightarrow{B}
 $K_{AB} := \text{elem}(1, \text{decrypt}(K_{BS}, M))$
 $R_B \in \text{new_nonce}$
 $(X, B, M) \quad \leftrightarrow \quad \text{Network}$
 $(\text{respond}, A) \quad \leftrightarrow \quad \text{State}_B$
 $(\text{new session key}, A, K_{AB}, R_B) \quad \leftrightarrow \quad \text{State}_B$
 $(B, A, (\text{encrypt}(K_{AB}, R_B))) \quad \leftrightarrow \quad \text{Network}$

SH Verification Tool:

```

def_trans_pattern B step_4
  (X,A,S,M,KBS,RB)
  (X,B,M) ? Network,
  ['respond',A] ? B_State,
  [A,'agent'] ? B_State,
  [S,'server'] ? B_State,
  (S,'sym',KBS) ? B_Symkeys,
  head(tail(decrypt(KBS,M))) = A,
  /* KAB = head(decrypt(KBS,M)), */
  /* RB ? new_nonce, */
  RB << new_nonce,
  (X,B,M) << Network,
  ['respond',A] << B_State,
  [new_session_key,A,head(decrypt(KBS,M)),RB] >> B_State,
  (B,A,encrypt(head(decrypt(KBS,M)), [RB])) >> Network;

```

The usage chosen for nonces in the tool notation is described in step 1. In the pattern above RA is bound to the list $[17]$, the single element of the multiset new_nonce , then the tail of RA (in this case the empty list) is put back into the multiset and the head of RA (in this case 17) is used in the further lines of the above pattern.

APA model (step 5a):

Variables: X, B, M, K_{AB}, R_B

$(X, A, M) \in \text{Network}$
 $(\text{new session key}, B, K_{AB}) \in \text{State}_A$
 \xrightarrow{A}
 $R_B := \text{elem}(1, \text{decrypt}(K_{AB}, M))$
 $(X, A, M) \quad \leftrightarrow \quad \text{Network}$
 $(\text{new session key}, B, K_{AB}) \quad \leftrightarrow \quad \text{State}_A$
 $(\text{session key}, B, K_{AB}) \quad \hookrightarrow \quad \text{State}_A$
 $(B, \text{sym}, K_{AB}) \quad \hookrightarrow \quad \text{Symkeys}_A$
 $(A, B, (\text{encrypt}(K_{AB}, (R_B - 1)))) \quad \hookrightarrow \quad \text{Network}$

SH Verification Tool:

```

def_trans_pattern A step_5a
  (X,B,M,KAB)
  (X,A,M) ? Network,
  ['new_session_key',B,KAB] ? A_State,
  /* RB = head(decrypt(KAB,M)), */
  (X,A,M) << Network,
  ['new_session_key',B,KAB] << A_State,
  ['session_key',B,KAB] >> A_State,
  (B,'sym',KAB) >> A_Symkeys,
  (A,B,encrypt(KAB,[head(decrypt(KAB,M))-1])) >> Network;

```

APA model (step 5b):

Variables: X, A, M, K_{AB}, R_B

$(X, B, M) \in \text{Network}$

$(\text{new session key}, A, K_{AB}, R_B) \in \text{State}_B$

$\text{elem}(1, \text{decrypt}(K_{AB}, M)) + 1 = R_B$

\xrightarrow{B}

$(X, B, M) \quad \leftrightarrow \quad \text{Network}$

$(\text{new session key}, A, K_{AB}, R_B) \quad \leftrightarrow \quad \text{State}_B$

$(\text{session key}, A, K_{AB}) \quad \hookrightarrow \quad \text{State}_B$

$(A, \text{sym}, K_{AB}) \quad \hookrightarrow \quad \text{Symkeys}_B$

SH Verification Tool:

```
def_trans_pattern B step_5b
(X,A,M,KAB,RB)
(X,B,M) ? Network,
['new_session_key',A,KAB,RB] ? B_State,
head(decrypt(KAB,M))+1 = RB,
(X,B,M) << Network,
['new_session_key',A,KAB,RB] << B_State,
['session_key',A,KAB] >> B_State,
(A,'sym',KAB) >> B_Symkeys;
```

APA model (newA):Variables: B, K_{AB} $(\text{session key}, B, K_{AB}) \in \text{State}_A$ \xrightarrow{A} $(\text{start}, B) \leftrightarrow \text{State}_A$ **SH Verification Tool:**

```
def_trans_pattern A newA
  (B,KAB)
  ['session_key',B,KAB] ? A_State,
  ['start',B] ~? A_State,
  ['start',B] >> A_State;
```

In the tool notation it is checked whether the element `['start',B]` is already in `A_State` to prevent an endless loop here.

APA model (newB):Variables: A, K_{AB} $(\text{session key}, A, K_{AB}) \in \text{State}_B$ \xrightarrow{B} $(\text{respond}, A) \leftrightarrow \text{State}_B$ **SH Verification Tool:**

```
def_trans_pattern B newB
  (A,KAB)
  ['session_key',A,KAB] ? B_State,
  ['respond',A] ~? B_State,
  ['respond',A] >> B_State;
```

In the tool notation it is checked whether the element `['respond',A]` is already in `B_State` to prevent an endless loop here.

SH Verification Tool: Reachability graph

The reachability graph computed by the SH Verification Tool for this configuration is shown in figures 3 and 4.

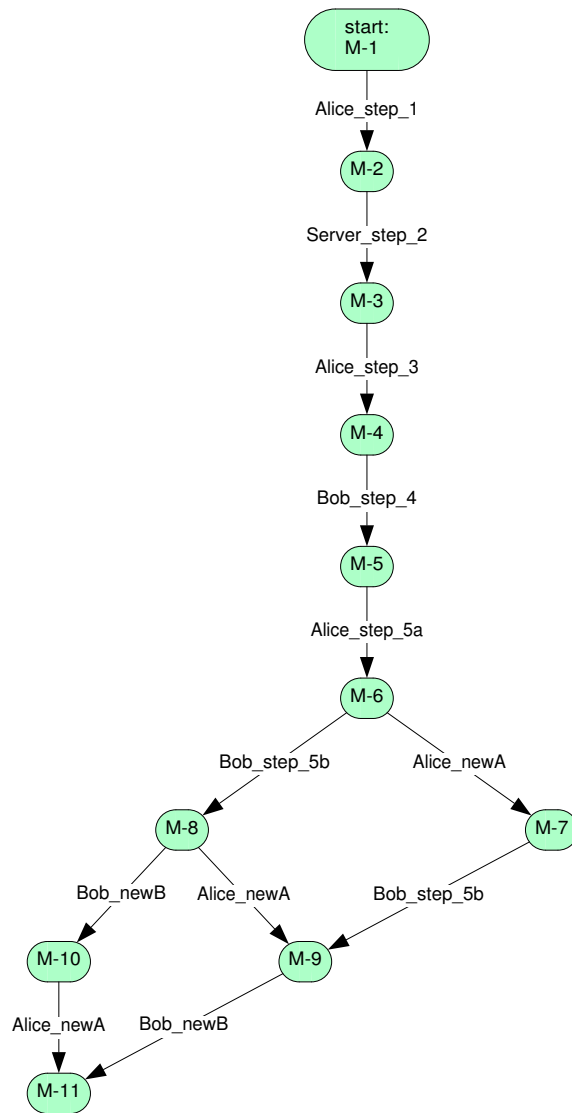


Figure 3: Reachability graph

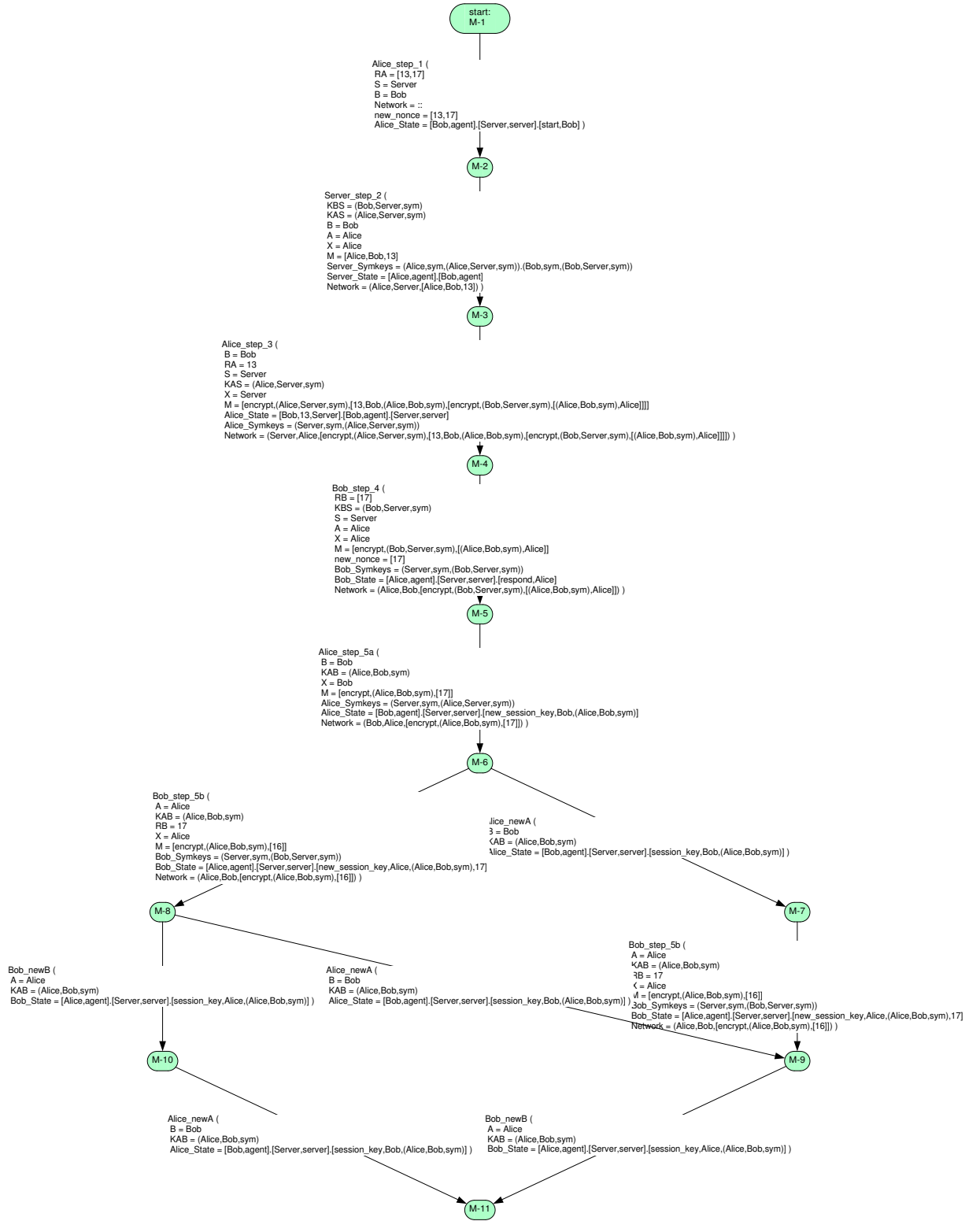


Figure 4: Reachability graph with interpretation

References

- [Fra02a] Fraunhofer Institute for Secure Telecooperation SIT, Darmstadt. *Simple Homomorphism Verification Tool – Manual*, 2002.
- [Fra02b] Fraunhofer Institute for Secure Telecooperation SIT, Darmstadt. *Simple Homomorphism Verification Tool – Tutorial*, 2002.
- [ORR00] P. Ochsenschläger, J. Repp, and R. Rieke. The SH-Verification Tool. In *Proc. 13th International FLorida Artificial Intelligence Research Society Conference (FLAIRS-2000)*, pages 18–22, Orlando, FL, USA, May 2000. AAAI Press.
- [SOR02] Gürgens S., P. Ochsenschläger, and Carsten Rudolph. Role based specification and analysis with APA. GMD Report 151, Fraunhofer Institute for Secure Telecooperation SIT, 2002.

Appendix

SH Verification Tool:

```
defset Agents = 'Alice', 'Alice2', 'Bob', 'Server' ;

defset Address = Agents;

defset Identity = Agents || nat_0;

defset Nonce = 13, 17, 19, 23;

defset Nonces = [Nonce];

defset Nonce_seq = seq(Nonces);

defset Run_seq = seq(nat_0);

defset Constants = 'start', 'respond', 'agent', 'server',
                  'new_session_key', 'session_key';

defset Symflags = 'sym', 'symmac';

defset Asymflags = 'pub', 'priv', 'pucipher', 'privcipher',
                  'pubverify', 'privsign';

defset Cryptfuncs = 'encrypt', 'decrypt', 'crypt', 'sign', 'mac', 'hash';

defset Keywords = Symflags || Asymflags || Constants || Cryptfuncs;

defset Skeys = pro(Agents, Agents, Symflags);

defset Akeys = pro(Agents, Asymflags);

defset Keys = Skeys || Akeys;

defset message = Keywords || Agents || Nonce || Keys || nat_0;
/* nat_0 wg. nonce -1 */

defset Messages = [message];

defset Messages_seq = seq(Messages);

defset Symkeys = pro(Identity, Symflags, Keys);

defset Asymkeys = pro(Identity, Asymflags, Keys);

defset Symkeys_seq = seq(Symkeys);

defset Asymkeys_seq = seq(Asymkeys);

defset net_elem = pro(Address, Address, Messages);

defset net_elem_seq = seq(net_elem);

defset nat0_seq = seq(nat_0);

def_state Network: net_elem_seq := :::
```



```

def_state new_nonce: Nonce_seq := [13,17];
/*
def_state new_nonce: Nonce_seq := [13,17,19,23];
*/
/*
def_state new_runs: Run_seq := 1;
*/
def_role A;

def_role B;

def_role S;

def_state A State: Messages_seq := [B,'agent'].[S,'server'].['start',B];

def_state A Symkeys: Symkeys_seq := (S,'sym',(A,S,'sym'));

def_state A Asymkeys: Asymkeys_seq := ::;

def_state B State: Messages_seq := [A,'agent'].[S,'server'].['respond',A];

def_state B Symkeys: Symkeys_seq := (S,'sym',(B,S,'sym'));

def_state B Asymkeys: Asymkeys_seq := ::;

def_state S State: Messages_seq := [A,'agent'].[B,'agent'];

def_state S Symkeys: Symkeys_seq := (A,'sym',(A,S,'sym')).
    (B,'sym',(B,S,'sym'));

def_state S Asymkeys: Asymkeys_seq := ::;

/*
defcase encrypt: pro(Keys,Messages) >> Messages
    encrypt(key,message) = if head(message) = 'decrypt' &
        head(tail(message)) = key
        then head(tail(tail(message)))
        else ['encrypt',key,message];
*/

defterm encrypt: pro(Keys,Messages) >> Messages
    encrypt(key,message) = ['encrypt',key,message];

defcase decrypt: pro(Keys,Messages) >> Messages
    decrypt(key,message) = if head(message) = 'encrypt' &
        head(tail(message)) = key
        then head(tail(tail(message)))
        else ['decrypt',key,message];

def_trans_pattern A step_1
    (RA,B,S)
    ['start',B] ? A_State,
    [B,'agent'] ? A_State,
    [S,'server'] ? A_State,
    RA << new_nonce,
    tail(RA) >> new_nonce,
    ['start',B] << A_State,
    [B,head(RA),S] >> A_State,
    (A,S,[A,B,head(RA)]) >> Network;

```

```

def_trans_pattern S step_2
(X,A,B,M,KAS,KBS)
(X,S,M) ? Network,
[A,'agent'] ? S_State,
A = head(M),
[B,'agent'] ? S_State,
B = head(tail(M)),
(A,'sym',KAS) ? S_Symkeys,
(B,'sym',KBS) ? S_Symkeys,
/* RA = head(tail(tail(M))),*/
(X,S,M) << Network,
(S,A,encrypt(KAS,[head(tail(tail(M))),B,(A,B,'sym'),
encrypt(KBS,[A,B,'sym'],A)])) >> Network;

def_trans_pattern A step_3
(X,B,S,M,KAS,RA)
(X,A,M) ? Network,
/* [B,RA,S] ? A_State,*/
(S,'sym',KAS) ? A_Symkeys,
head(decrypt(KAS,M)) = RA,
head(tail(decrypt(KAS,M))) = B,
[B,RA,S] ? A_State,
/* KAB = head(tail(tail(decrypt(KAS,M))))),*/
/* Chiffretext = head(tail(tail(tail(decrypt(KAS,M))))),*/
(X,A,M) << Network,
[B,RA,S] << A_State,
[new_session_key,B,head(tail(tail(decrypt(KAS,M))))] >> A_State,
(A,B,head(tail(tail(tail(decrypt(KAS,M)))))) >> Network;

def_trans_pattern B step_4
(X,A,S,M,KBS,RB)
(X,B,M) ? Network,
['respond',A] ? B_State,
[A,'agent'] ? B_State,
[S,'server'] ? B_State,
(S,'sym',KBS) ? B_Symkeys,
head(tail(decrypt(KBS,M))) = A,
/* KAB = head(decrypt(KBS,M)),*/
/* RB ? new_nonce,*/
RB << new_nonce,
tail(RB) >> new_nonce,
(X,B,M) << Network,
['respond',A] << B_State,
[new_session_key,A,head(decrypt(KBS,M)),head(RB)] >> B_State,
(B,A,encrypt(head(decrypt(KBS,M)),[head(RB)])) >> Network;

def_trans_pattern A step_5a
(X,B,M,KAB)
(X,A,M) ? Network,
['new_session_key',B,KAB] ? A_State,
/* RB = head(decrypt(KAB,M)),*/
(X,A,M) << Network,
['new_session_key',B,KAB] << A_State,
['session_key',B,KAB] >> A_State,
(B,'sym',KAB) >> A_Symkeys,
(A,B,encrypt(KAB,[head(decrypt(KAB,M))-1])) >> Network;

def_trans_pattern B step_5b
(X,A,M,KAB,RB)
(X,B,M) ? Network,
['new_session_key',A,KAB,RB] ? B_State,
head(decrypt(KAB,M))+1 = RB,

```

```

(X,B,M) << Network,
['new_session_key',A,KAB,RB] << B_State,
['session_key',A,KAB] >> B_State,
(A,'sym',KAB) >> B_Symkeys;

def_trans_pattern A newA
(B,KAB)
['session_key',B,KAB] ? A_State,
['start',B] ~? A_State,
['start',B] >> A_State;

def_trans_pattern B newB
(A,KAB)
['session_key',A,KAB] ? B_State,
['respond',A] ~? B_State,
['respond',A] >> B_State;

def_pattern_bind A := 'Alice' ;

def_pattern_bind B := 'Bob' ;
/*
def_pattern_bind B := 'Alice2', 'Bob' ;
*/
def_pattern_bind S := 'Server' ;

```